# Overpersistence Bias in Individual Income Expectations and its Aggregate Implications 

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## Motivation

Households make decisions under uncertainty
$\rightarrow$ income risk is one of the most important sources of risk
Income expectations important for

- consumption vs savings
- durable vs non-durable consumption


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$\rightarrow$ income risk is one of the most important sources of risk
Income expectations important for

- consumption vs savings
- durable vs non-durable consumption


## This paper:

(1) What are typical features of household income expectations?
(2) How do these features affect consumption/savings choices? Aggregate Implications?

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1) household income expectations in micro data:

- construct expectation errors on individual household level
- systematic bias: current income predicts expectation error households overestimate persistence


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- partial equilibrium model with durable and non-durable consumption
- allowing for biased income expectations
$\Rightarrow$ overpersistence bias: model can fit joint distribution of income and liquid assets!


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2) effects of household income expectations on consumption choices:

- partial equilibrium model with durable and non-durable consumption
- allowing for biased income expectations
$\Rightarrow$ overpersistence bias: model can fit joint distribution of income and liquid assets!

3) aggregate implications:

- MPC of low income households lower under biased expectations
$\Rightarrow$ fiscal transfers less effective!


## Roadmap

1) Household Expectations in Micro Data
(a) Data \& Interview time structure
(b) Expectation Errors in the Cross-Section: Overpersistence
(c) Expectation about Aggregates
2) Model
(a) Income process and Expectations errors
(b) Consumption
3) Results
(a) Distributions by Income Group
(b) MPC and effectiveness of transfer policies
(c) Alternative Borrowing Constraints

## Data

## Michigan Survey of Consumers

## Survey characteristics:

- 500 observations each month (micro data since 1987M7)
- content: household characteristics, expectations about unemployment, inflation, interest rates, purchasing conditions and individual income expectations
- mix of repeated cross-section and short panel:
- short panel dimension: $1 / 3$ re-interviewed after 6 months


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Forecast Errors:

$$
\psi_{i, t}=\hat{g}_{i, t+1 \mid t}-g_{i, t+1}
$$

where

$$
g_{i, t+1}=Y_{i, t+1} / Y_{i, t}
$$

## Interview time structure: Ideal

Data


## Interview time structure: Ideal

 Data- First interview: January 2002



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## Interview time structure: Ideal

- First interview: January 2002
- Perfect overlap of expected and realised $g$ :

$$
\psi_{i, t}=\hat{g}_{i, t+1 \mid t}-g_{i, t+1}
$$



## Interview time structure

- Aim: compare expectation with realization
- Challenge:
- 6 months between interviews
- time structure of expectations vs realizations
- expectations: expected income growth in next 12 months
- income realization: total household income in last calendar year


## Interview time structure: Reality

Data
Two problems:

First interview: January 2002


## Interview time structure: Reality

Data
Two problems:

- re-interviews after 6 months

First interview: January 2002


## Interview time structure: Reality

Data
Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: January 2002


## Interview time structure: Reality

Data
Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: February 2002


## Interview time structure: Reality

Data
Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: March 2002


## Interview time structure: Reality

Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: April 2002


## Interview time structure: Reality

Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: May 2002


## Interview time structure: Reality

Data
Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: June 2002


## Interview time structure: Reality

Data
Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: July 2002


## Interview time structure: Reality

Data
Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: July 2002
(partial) overlap! ... © (results coming)


## Interview time structure: Reality

Data
Two problems:

- re-interviews after 6 months
- past income in calendar year

First interview: December 2002

Reality strikes back! ... ©


## Interview time structure: Imputation

Data
Use other people to impute missing income information First interview in second half of year $\rightarrow$ two years of income data


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\hat{Y}_{i, t+1}=f\left(Y_{i, t}, \Gamma_{i}\right)
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Use this to impute income realizations:

- Best case: (first interview in) January - perfect overlap



## Interview time structure: Imputation

Use other people to impute missing income information
First interview in second half of year $\rightarrow$ two years of income data
Estimate

$$
\hat{Y}_{i, t+1}=f\left(Y_{i, t}, \Gamma_{i}\right)
$$

Use this to impute income realizations:

- Best case: January - perfect overlap
- Worst case: June - 7/12 overlapping



## Interview time structure: Robustness

## Specifications:

- baseline: realizations imputed, all months

$$
\begin{aligned}
\rightarrow \text { advantage: } & \text { - increases overlap } \\
& \text { - maximizes observations }
\end{aligned}
$$

- robustness:
- July only, directly reported data: no imputation
- January only, imputed: perfect overlap


## Forecast Errors in Real Income Growth

Figure: Mean forecast error


## Forecast Errors in Real Income Growth

Figure: Mean forecast error by income

observation: - low income households too pessimistic

- high income households too optimistic


## Forecast Errors on Observables

|  | (1) <br> real | (2) real | (3) real | (4) nominal | (5) <br> inflation |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Income Quintile |  |  |  |  |  |
| 1 (low) | $-0.052^{* * *}$ | -0.046 ** | $-0.075^{* * *}$ | $-0.049^{* * *}$ | 0.004*** |
|  | (0.006) | (0.018) | (0.021) | (0.007) | (0.000) |
| 2 | $-0.018^{* *}$ | -0.013 | -0.038* | $-0.016^{* * *}$ | 0.002*** |
|  | (0.006) | (0.017) | (0.020) | (0.006) | (0.000) |
| 4 | 0.019*** | 0.026* | 0.025 | 0.018*** | -0.002*** |
|  | (0.005) | (0.013) | (0.016) | (0.005) | (0.000) |
| 5 (high) | 0.035*** | 0.046*** | 0.067*** | 0.032*** | $-0.004^{* * *}$ |
|  | (0.006) | (0.015) | (0.017) | (0.006) | (0.000) |
| Education (0.00) |  |  |  |  |  |
| no high school | 0.014 | 0.015 | 0.000 | 0.019 | 0.002** |
|  | (0.013) | (0.029) | (0.036) | (0.013) | (0.001) |
| college | $-0.014^{* * *}$ | $-0.024 * *$ | $-0.032^{* *}$ | $-0.017^{* * *}$ | $-0.003 * * *$ |
|  | (0.004) | (0.012) | (0.013) | (0.004) | (0.000) |
| Age |  |  |  |  |  |
| age | $-0.004^{* * *}$ | -0.003 | -0.006 | $-0.004^{* * *}$ | 0.000*** |
|  | (0.001) | (0.003) | (0.004) | (0.002) | (0.000) |
| age $\times$ age | 0.000** | 0.000 | 0.000 | 0.000* | $-0.000 * * *$ |
|  | (0.000) | (0.000) | (0.000) | (0.000) | (0.000) |
| Sample Imputation Observations | MAIN | JAN | JULY | MAIN | INF |
|  | yes | yes | no | yes | no |
|  | 58369 | 6973 | 2805 | 58369 | 88017 |

* $p<0.1$, ** $p<0.05$, *** $p<0.01$. Standard errors in parentheses.
additional controls: ethnic background, number of adults, gender, marriage status, region, month, constant


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## Forecast Errors in Real Income Growth

Figure: Mean forecast errors by income

$\rightarrow$ robust to controlling for household characteristics!

## Overpersistence Bias

Mechanism

## Assumption

- Individual income $Y$ has transitory $(T)$ and persistent $(P)$ component ${ }^{1}$
- Households overestimate persistence in P


## Theorem

(a) $\exists!\bar{P}$ :

$$
E\left[\log \left(Y_{i t+1 \mid t}\right)-\log \left(Y_{i t+1}\right) \mid P_{i t}>\bar{P}\right]>0
$$

and vice versa for $P_{i t}<\bar{P}$
(b) let $\Delta_{i t} \equiv P_{i t}-\bar{P}$, then

$$
\frac{\partial E\left[\log \left(Y_{i t+1 \mid t}\right)-\log \left(Y_{i t+1}\right) \mid \Delta_{i t}\right]}{\partial \Delta_{i t}}>0
$$

[^0]
## Overpersistence Bias

Intuition


## Overpersistence Bias

Intuition
Persistent shocks decay over time example $\operatorname{AR}(1): P_{t+1}=\rho P_{t}+\varepsilon_{t+1}$


## Overpersistence Bias

Intuition
Persistent shocks decay over time more persistence (larger $\rho$ ) $\rightarrow$ slower decay


## Overpersistence Bias

Intuition
Persistent shocks decay over time more persistence (larger $\rho$ ) $\rightarrow$ slower decay $\Rightarrow$ good shocks $\rightarrow$ optimism


## Overpersistence Bias

Persistent shocks decay over time more persistence (larger $\rho$ ) $\rightarrow$ slower decay $\Rightarrow$ bad shocks $\rightarrow$ pessimism


## Overpersistence Bias

Intuition
Persistent shocks decay over time more persistence (larger $\rho$ ) $\rightarrow$ slower decay $\Rightarrow$ one parameter $\rightarrow$ heterogenous error sign


## Forecast Errors in Aggregates

Figure: Forecast errors in inflation by income


- people overestimate inflation across the whole income distribution
- similar to unemployment expectations = too pessimistic across whole income distribution


## Summary Empirical Findings

(1) Overpersistence Bias in Income Expectations:

- low income households too pessimistic
- high income households too optimistic
(2) Aggregate Pessimism:
all income groups too pessimistic about aggregates


## Modeling income and expectations

## Income process

Model

$$
Y_{i t}=Z_{t} \cdot P_{i t} \cdot T_{i t}
$$

## Income process

Model

$$
Y_{i t}=Z_{t} \cdot P_{i t} \cdot T_{i t}
$$

- transitory shock:

$$
T_{i t} \sim \log N\left(-\frac{\sigma_{T}^{2}}{2}, \sigma_{T}^{2}\right)
$$

# Income process 

Model

$$
Y_{i t}=Z_{t} \cdot P_{i t} \cdot T_{i t}
$$

- persistent idiosyncratic shock:

$$
\log P_{i t}=\rho \log P_{i t-1}+\epsilon_{i t}^{P}, \quad \epsilon_{i t}^{P} \sim N\left(0, \sigma_{P}^{2}\right)
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# Income process 

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Overpersistence Bias:

$$
\log P_{i t}=\hat{\rho} \log P_{i t-1}+\epsilon_{i t}^{P}, \quad \epsilon_{i t}^{P} \sim N\left(0, \sigma_{P}^{2}\right)
$$

$\rightarrow$ find $\hat{\rho}$ to match the observed forecasting errors

## Income process

Model

$$
Y_{i t}=Z_{t} \cdot P_{i t} \cdot T_{i t}
$$

- persistent aggregate state:

$$
\mathbb{Z}=\left[\begin{array}{c}
Z^{h} \\
Z^{\prime}
\end{array}\right], \quad \Pi_{Z}=\left[\begin{array}{cc}
\pi_{11} & 1-\pi_{11} \\
1-\pi_{22} & \pi_{22}
\end{array}\right]
$$

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Aggregate Pessimism:

$$
\hat{Z}_{t+1 \mid t}=\mu \cdot \mathrm{E} Z_{t+1}=\mu \cdot \Pi_{Z}\left(Z_{t}\right) \mathbb{Z}
$$

## Parameters of the income process

Calibration

| Parameter |  | Value |
| :--- | :---: | :---: |
| persistence of idiosyncratic income process | $\rho$ | 0.9774 |
| std dev of idiosyncratic persistent shocks | $\sigma_{P}$ | 0.0424 |
| std dev of idiosyncratic transitory shocks | $\sigma_{V}$ | 0.1 |
| high aggregate income state | $Z^{h}$ | 1.0040 |
| low aggregate income state | $Z^{\prime}$ | 0.9790 |
| prob. of entering recession | $1-\pi_{11}$ | $6.85 \%$ |
| prob. of leaving recession | $1-\pi_{22}$ | $36.04 \%$ |

$\rho, \sigma_{P}, \sigma_{T}$ : Storesletten et al. (2004); Berger and Vavra (2015)
$Z$ : NBER recessions vs booms frequencies and average HPF GDP deviation

## Replicating forecasting errors

Model
Overpersistence bias (fitted): $\quad \hat{\rho}=0.9831$, (true $\rho=0.9774$ )
Aggregate pessimism (fitted): $\quad \mu=0.9778$

Table: Mean expectation errors in income growth

|  | data | model |
| :---: | :---: | :---: |
| income quintile 1 | -0.072 | -0.068 |
| income quintile 2 | -0.037 | -0.040 |
| income quintile 3 | -0.019 | -0.021 |
| income quintile 4 | -0.000 | -0.004 |
| income quintile 5 | 0.016 | 0.020 |

## Modeling consumption

## Overview

- partial equilibrium analysis, infinite horizon
- household obtains utility from two goods:
- non-durable consumption
- durable good
- household can invest in two assets:
- durable good: adjustment costs \& depreciation
- liquid asset: earns risk-free interest
$\rightarrow$ borrowing possible at higher interest rate
- only source of risk: exogenous income


## Household Optimization Problem

Model

$$
\max _{\left\{c_{t}\right\}_{t=0}^{\infty},\left\{d_{t}\right\}_{t=0}^{\infty},\left\{s_{t}\right\}_{t=0}^{\infty}} \mathrm{E} \sum_{t=0}^{\infty} \beta^{t} U\left(c_{t}, d_{t}\right)
$$

s.t. $\quad c_{t}+d_{t}+s_{t}+A\left(d_{t}, d_{t-1}\right) \leq R\left(s_{t-1}\right)+Y_{t}+(1-\delta) d_{t-1}$

## Household Optimization Problem

Model

$$
\max _{\left\{c_{t}\right\}_{t=0}^{\infty},\left\{d_{t}\right\}_{t=0}^{\infty},\left\{s_{t}\right\}_{t=0}^{\infty}} \mathrm{E} \sum_{t=0}^{\infty} \beta^{t} U\left(c_{t}, d_{t}\right)
$$

s.t. $\quad c_{t}+d_{t}+s_{t}+A\left(d_{t}, d_{t-1}\right) \leq R\left(s_{t-1}\right)+Y_{t}+(1-\delta) d_{t-1}$

$$
U(c, d)=\frac{\left[\left((1-\theta) c^{\frac{\xi-1}{\xi}}+\theta(\bar{d}+d)^{\frac{\xi-1}{\xi}}\right)^{\frac{\xi}{\xi-1}}\right]^{1-\gamma}}{1-\gamma}
$$

## Household Optimization Problem

Model

$$
\max _{\left\{c_{t}\right\}_{t=0}^{\infty},\left\{d_{t}\right\}_{t=0}^{\infty},\left\{s_{t}\right\}_{t=0}^{\infty}} \mathrm{E} \sum_{t=0}^{\infty} \beta^{t} U\left(c_{t}, d_{t}\right)
$$

s.t. $\quad c_{t}+d_{t}+s_{t}+A\left(d_{t}, d_{t-1}\right) \leq R\left(s_{t-1}\right)+Y_{t}+(1-\delta) d_{t-1}$

$$
A\left(d_{t}, d_{t-1}\right)= \begin{cases}0 & \text { if } d_{t}=(1-\delta) d_{t-1} \\ F^{d}(1-\delta) d_{t-1} & \text { otherwise }\end{cases}
$$

## Household Optimization Problem

Model

$$
\max _{\left\{c_{t}\right\}_{t=0}^{\infty},\left\{d_{t}\right\}_{t=0}^{\infty},\left\{s_{t}\right\}_{t=0}^{\infty}} \mathrm{E} \sum_{t=0}^{\infty} \beta^{t} U\left(c_{t}, d_{t}\right)
$$

s.t. $c_{t}+d_{t}+s_{t}+A\left(d_{t}, d_{t-1}\right) \leq R\left(s_{t-1}\right)+Y_{t}+(1-\delta) d_{t-1}$

$$
Y_{i t}=Z_{t} \cdot P_{i t} \cdot T_{i t}
$$

- Components to income:
- aggregate persistent ( $Z$ )
- idiosyncratic persistent ( $P$ )
- idiosyncratic transitory ( $T$ )


## Household Optimization Problem

Model

$$
\max _{\left\{c_{t}\right\}_{t=0}^{\infty},\left\{d_{t}\right\}_{t=0}^{\infty},\left\{s_{t}\right\}_{t=0}^{\infty}} \mathrm{E} \sum_{t=0}^{\infty} \beta^{t} U\left(c_{t}, d_{t}\right)
$$

s.t. $\quad c_{t}+d_{t}+s_{t}+A\left(d_{t}, d_{t-1}\right) \leq R\left(s_{t-1}\right)+Y_{t}+(1-\delta) d_{t-1}$

$$
R\left(s_{t}\right)=\left[1+r\left(s_{t}\right)\right] s_{t}, \text { where } r\left(s_{t}\right)= \begin{cases}r^{\prime} & \text { if } s_{t}>0 \\ r^{b} & \text { if }-\left(\kappa_{y} P_{t}+\kappa_{d} d_{t}\right) \leq s_{t} \leq 0\end{cases}
$$

## Parameters of the Environment

Calibration

| Parameter |  | Value |
| :--- | :---: | :---: |
| interest rate (lending) | $r^{\prime}$ | 0.0016 |
| interest rate (borrowing) | $r^{b}$ | 0.02 |
| loan-to-income constraint | $\kappa_{y}$ | 0.56 |
| loan-to-value constraint | $\kappa_{d}$ | 0.8 |
| depreciation rate | $\delta$ | 0.05 |
| adjustment costs | $F^{d}$ | 0.3 |

## Belief and Preference Parameters

Calibration

| Parameter |  | Value |
| :--- | :---: | :---: |
| beliefs: |  |  |
| $\quad$ persistence of $P$ | $\rho$ | 0.9831 |
| $\quad$ pessimism | $\mu$ | 0.9778 |
| preferences: |  |  |
| $\quad$ discount factor | $\beta$ | 0.9825 |
| risk aversion | $\gamma$ | 1.5 |
| weight of durable goods in utility | $\theta$ | 0.075 |
| elasticity of substitution in utility | $\underline{\xi}$ | 3 |
| free durable services | $d$ | 0.5 |

## Preferences parameters

Calibration

(a) d, aggregate

(b) s, aggregate

## Results

## Distribution of durable stock

Results

Figure: Durable stock $d$ by income

(a) first quintile

(b) fifth quintile
observation: durables not much affected by bias

## Distribution of liquid savings

Results
Figure: Liquid savings $s$ by income

(a) first quintile

(b) fifth quintile
observation: low income households borrow less
$\rightarrow$ do not borrow even though borrowing constraint not binding!

## Propensity to Consume

Results

Figure: MPC out of unexpected transfer (non-durable goods)


## Propensity to Consume

Results

Figure: MPC out of unexpected transfer (non-durable goods)

observation: - overall: lower MPC with biased expectations - low income: lower MPC with biased expectations

## Propensity to Consume

Results

|  | model |  | data |  |
| :--- | :---: | :---: | :---: | :---: |
|  | biased beliefs | rational beliefs | stimulus 2001 ${ }^{1}$ | stimulus $2008^{2}$ |
| low/high | 1.94 | 2.86 | 2.33 | 1.16 |

observation: model with rational beliefs overestimates ratio of MPCs (low to high income)
$\rightarrow$ overestimates effectiveness of fiscal stimulus!
${ }^{1}$ Johnson, Parker and Souleles (AER 2006)
${ }^{2}$ Parker, Souleles, Johnson and McClelland (AER 2013)

## Alternative Borrowing Constraints

overpersistence bias can explain why households don't borrow more alternative way to avoid large borrowing: tighter borrowing constraints

- benchmark model:

$$
s_{t} \geq-\left(\kappa_{y} P_{t}+\kappa_{v} d_{t}\right)
$$

- alternative:

$$
s_{t} \geq-\underline{s}, \quad \underline{s} \in[0,4]
$$

## Alternative Borrowing Constraints

Results
Figure: Liquid savings for different borrowing constraints

observation:

- tightening the borrowing limit increases share with positive assets
- rational agents especially responsive to borrowing limit


## Alternative Borrowing Constraints

Results

Figure: Liquid savings for different borrowing constraints

(a) Aggregate MPC

(b) relative MPC
observation: borrowing limit strongly affects MPC!
$\rightarrow$ choice of mechanism that avoids borrowing is not innocuous!

## Summary

1) household income expectation in micro data:

- data: Michigan Survey of Consumers
- findings: current income predicts expectation error
- interpretation: households overestimate persistence of income

2) model of durable and non-durable consumption:

- partial equilibrium model, allowing for overpersistence bias
- overpersistence bias: low income households do not want to borrow even though they could
$\Rightarrow$ allows model to fit low end of liquid asset distribution!

3) aggregate implications:

- MPC smaller for low income households
$\Rightarrow$ model with rational expectations overestimates effectiveness of stimulus


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## Literature

Household expectations:

- expectations about aggregates:
- inflation: Carroll (2003), Andolfatto et al. (2008), Malmendier and Nagel (2015), Coibion et al. (2015) etc.
- house prices: Gerardi et al. (2008), Piazzesi and Schneider (2009), Case et al. (2012) etc.
- excess bond returns: Piazzesi et al. (2015)
- credit spreads: Bordalo et al. (2017)
- individual income expectations:

Dominitz and Manski (1997), Dominitz (1998), Das and van Soest (1999), Souleles (2004)

Structural models of consumption:

- Kaplan and Violante (2014)
- Berger and Vavra (2015)


## Questions about Income Expectations

- income:
- Q1a: During the next 12 months, do you expect your income to be higher or lower than during the past year?
- Q1b: By about what percent do you expect your income to (increase/decrease) during the next 12 months?
- inflation:
- Q2a: During the next 12 months, do you think that prices in general will go up, or go down, or stay where they are now?
- Q2b: By about what percent do you expect prices to go (up/down) on the average, during the next 12 months?


## Imputation \& Comparison to PSID

Table: Distribution of reported income changes and imputed values

|  | mean | p5 | p25 | p50 | p75 | p95 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| directly reported | 0.034 | -0.378 | -0.097 | -0.015 | 0.133 | 0.572 |
| imputed | 0.032 | -0.365 | -0.103 | -0.016 | 0.130 | 0.577 |



## Forecast Errors in Real Income Growth

Figure: Mean income growth

(a) expectations

(b) realisations

## Forecast Errors in Nominal Income <br> Growth


(a) mean nominal error

(b) nominal error by income

## Alternative Mechanisms - not consistent with data

- Learning:
not consistent: forecast errors do not improve with age

```
\(\rightarrow\) graph
```

- Extrapolation of Recent Past:
not consistent: income expectations do not extrapolate from recent income growth regession
- Unobservable: Persistent vs Transitory Shocks: not consistent: cannot generate systematic bias based on past shock realizations (Kalman Filtering (also conditionally) optimal and unbiased)
- Systematically Wrong Expectations about Aggregates: not consistent: across income distribution households too pessimistic about aggregates (inflation and unemployment rate)
- Measurement noise quantitatively not strong enough


## Forecast Errors By Age

Figure: Forecast errors by age

observation: forecast errors do not improve with age!

## Extrapolation of recent Past?

|  | (1) exp. growth (real) | (2) exp. growth (real) | (3) exp. growth (nominal) | (4) exp. growth (nominal) |
| :---: | :---: | :---: | :---: | :---: |
| past expectation | $0.372^{* * *}$ | $0.374^{* * *}$ | $0.373^{* * *}$ | $0.374^{* * *}$ |
|  | (0.016) | (0.016) | (0.016) | (0.016) |
| past realized growth |  | $-0.021^{* * *}$ |  | -0.022*** |
|  |  | (0.004) |  | (0.004) |
| Income Quintile |  |  |  |  |
| 1st | 0.004 | 0.007 | 0.007 | 0.009** |
|  | (0.004) | (0.004) | (0.004) | (0.004) |
| 2nd | 0.002 | 0.003 | 0.004 | 0.005 |
|  | (0.004) | (0.004) | (0.004) | (0.004) |
| 4th | -0.005 | $-0.006^{*}$ | -0.005 | $-0.006^{*}$ |
|  | (0.004) | (0.004) | (0.003) | (0.003) |
| 5th | -0.008** | -0.010** | -0.008** | -0.010** |
|  | (0.004) | (0.004) | (0.004) | (0.004) |
| Constant | $0.061^{* * *}$ | 0.059*** | 0.070*** | 0.068*** |
|  | (0.022) | (0.022) | (0.022) | (0.021) |
| Observations | 15931 | 15931 | 17210 | 17210 |
| $R^{2}$ | 0.185 | 0.187 | 0.182 | 0.184 |

observation: households do not extrapolate from recent past!

## Parametrization

- $r^{\prime}=0.0016$ : mean real interest rate on 3 month treasury bills
- $r^{b}=0.02$ : credit cards and on auto loans
- $\kappa_{y}, \kappa_{v}$ : SCF borrowing limit credit card in 1992-2010, $80 \%$ of durables (average financing share at purchase $=0.78$ according to Attanasio et al. (2008))
- $F^{d}, \delta: 30 \%$ lost a new car resell, 10 years lifetime of a car
- $\rho, \sigma_{P}, \sigma_{T}$ : Storesletten, Telmer and Yaron (2004)
- Z: NBER recessions vs booms frequencies and average HPf GDP deviation


## Definition Liquid Assets

sample: car owners, Survey of Consumer Finances (SCF) 1992-2010
liquid assets:

- checking accounts
- savings accounts
- stocks, bonds, mututal funds, brokerage accounts
-     - credit card debt outstanding
-     - car loan outstanding


## Model Calibrated for Rational Agents

Results

Figure: Liquid savings $s$ by income

(a) aggregate

(b) first quintile
observation: results hold for model calibrated for rational expectations!


[^0]:    ${ }^{1} T$ : lognormal, $P: \mathrm{AR}(1)$ in logs with normal innovations

